

八皇后问题. Eight Queens

Turnpike Reconstruction Problem

Given $n(n-1)/2$ distances, reconstruct a point set.

Given $D = \{ 1, 2, 2, 2, 3, 3, 3, 4, 5, 5, 5, 6, 7, 8, 10 \}$.

① $n(n-1)/2 = 15$, $n = 6$.

② $x_1 = 0$, $x_6 = 10$.

③ find the next largest distance and check.

```
bool Reconstruct ( DistType X[ ], DistSet D, int N, int left, int right )
```

```

{ /* X[1]...X[left-1] and X[right+1]...X[N] are solved */
  bool Found = false;
  if ( Is_Empty( D ) )
    return true; /* solved */
  D_max = Find_Max( D );
  /* option 1: X[right] = D_max */
  /* check if |D_max-X[i]| ∈ D is true for all X[i]'s that have been solved */
  OK = Check( D_max, N, left, right ); /* pruning */
  if ( OK ) { /* add X[right] and update D */
    X[right] = D_max;
    for ( i=1; i<left; i++ ) Delete( |X[right]-X[i]|, D );
    for ( i=right+1; i<=N; i++ ) Delete( |X[right]-X[i]|, D );
    Found = Reconstruct ( X, D, N, left, right-1 );
    if ( !Found ) { /* if does not work, undo */
      for ( i=1; i<left; i++ ) Insert( |X[right]-X[i]|, D );
      for ( i=right+1; i<=N; i++ ) Insert( |X[right]-X[i]|, D );
    }
  }
  /* finish checking option 1 */
  if ( !Found ) { /* if option 1 does not work */
    /* option 2: X[left] = X[N]-D_max */
    OK = Check( X[N]-D_max, N, left, right );
    if ( OK ) {
      X[left] = X[N] - D_max;
      for ( i=1; i<left; i++ ) Delete( |X[left]-X[i]|, D );
      for ( i=right+1; i<=N; i++ ) Delete( |X[left]-X[i]|, D );
      Found = Reconstruct ( X, D, N, left+1, right );
      if ( !Found ) {
        for ( i=1; i<left; i++ ) Insert( |X[left]-X[i]|, D );
        for ( i=right+1; i<=N; i++ ) Insert( |X[left]-X[i]|, D );
      }
    }
    /* finish checking option 2 */
  }
  /* finish checking all the options */
}

```

如没找到下一个 8 (next large).

∴ 从最大开始取 (max-X[i]) 就是最小)

$x_5 = 8$.

∴ 最大、小两端已处理好.

现在已有 x_1, x_6 .

找 $|x_5 - x_1|, |x_5 - x_6|$ 存在

在 D 中

存在的话在 D 中划掉.

不存在的话 false 返回.

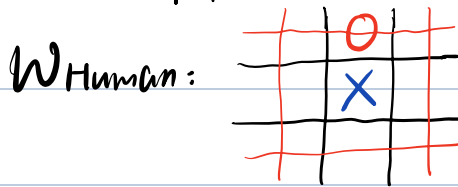
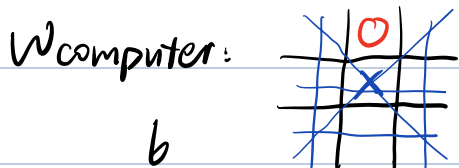
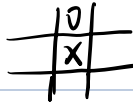
```
return Found;
```

Tic-tau-toe.

goodness of a position: $f(P) = W_{\text{computer}} - W_{\text{human}}$.

W : 在当前状况下可能可以实现之连接分数.

X computer, O human.



Human 想要 minimize, Alpha-Go 想要 maximize.

α - β pruning α - β 剪枝.

对应搜索, 就是让不能一直往同一个方向.

